## Bernard DACOROGNA (EPFL)

"Symplectic decomposition, Darboux theorem and ellipticity"

Our first result concerns the classical Darboux theorem. We prove that if  $\omega_m$  is the standard symplectic form and f is any symplectic form, then we can find a diffeomorphism  $\varphi$ , with optimal regularity, satisfying

$$\varphi^*(\omega_m) = f \text{ and } \langle \nabla \varphi; \omega_m \rangle = 0$$

provided that f is a small perturbation of  $\omega_m$ . Moreover we show that the above system is elliptic and that we have uniqueness, when coupled with a Dirichlet datum.

We then apply the above result to the so-called symplectic decomposition. We show that any map  $\varphi$ , satisfying appropriate assumptions, can be written as

 $\varphi = \chi \circ \psi$ 

where

$$\langle \nabla \chi; \omega_m \rangle = 0, \quad \nabla \varphi + (\nabla \varphi)^t > 0 \quad \text{and} \quad \psi^*(\omega_m) = \omega_m$$

The analogy with mass transportation and the Monge-Ampère equation, as well as with the polar decomposition, will be emphasized.

This is a joint work with Wifrid GANGBO and Olivier KNEUSS.